

COMSOL SETKÁNÍ UŽIVATELŮ



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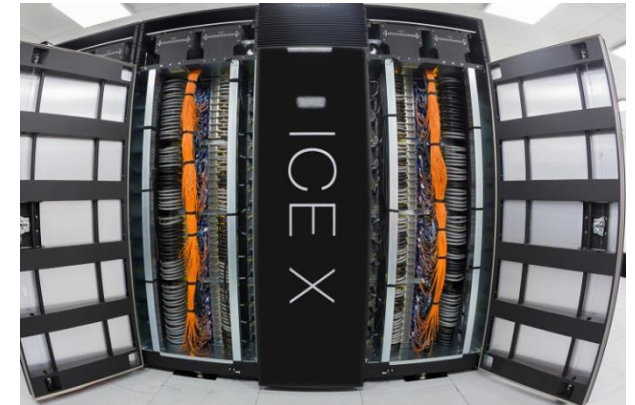
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Experimental research



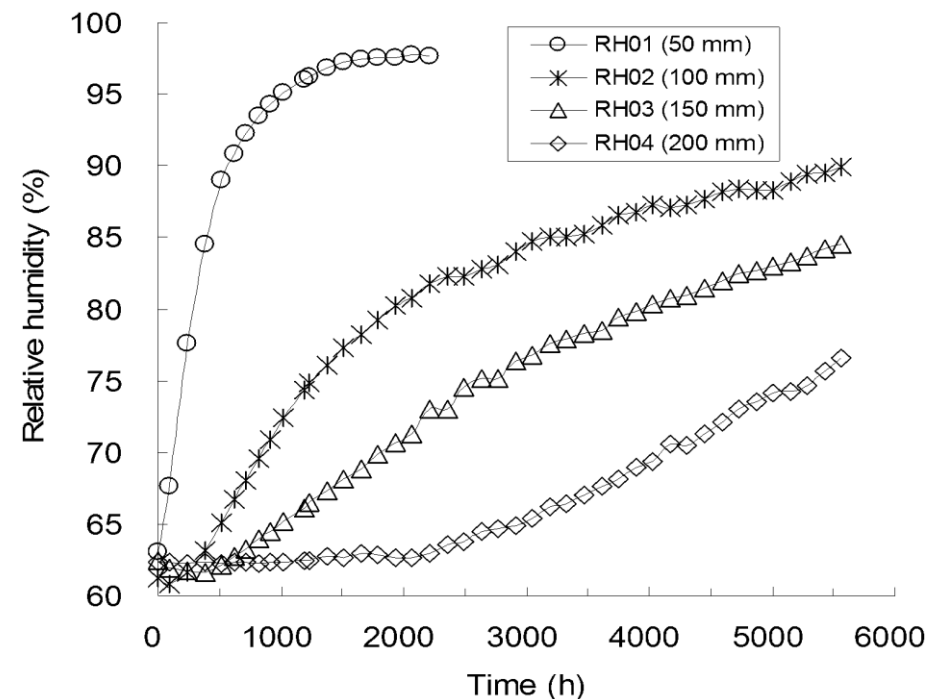
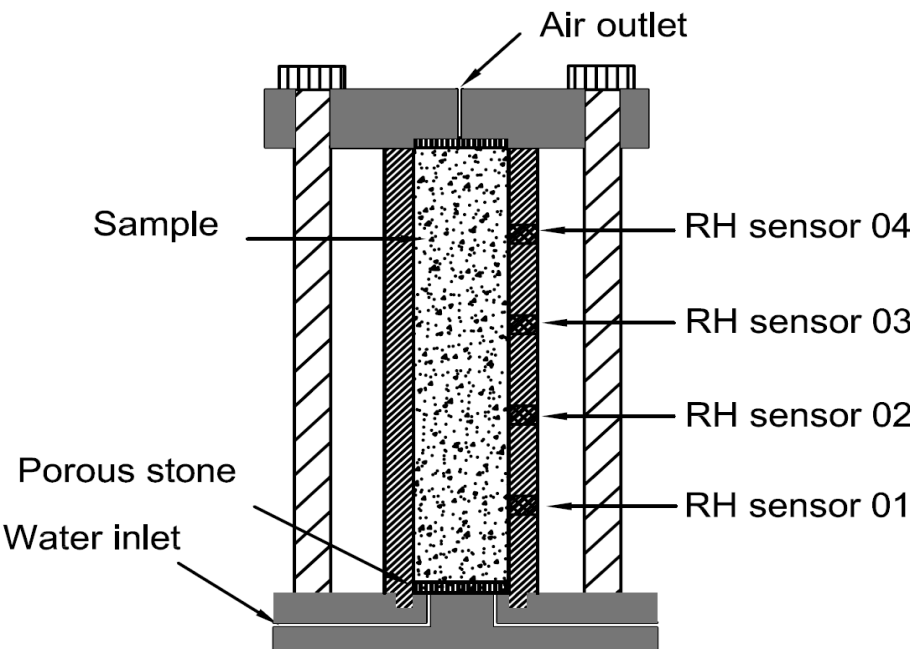
Modelling THM processes

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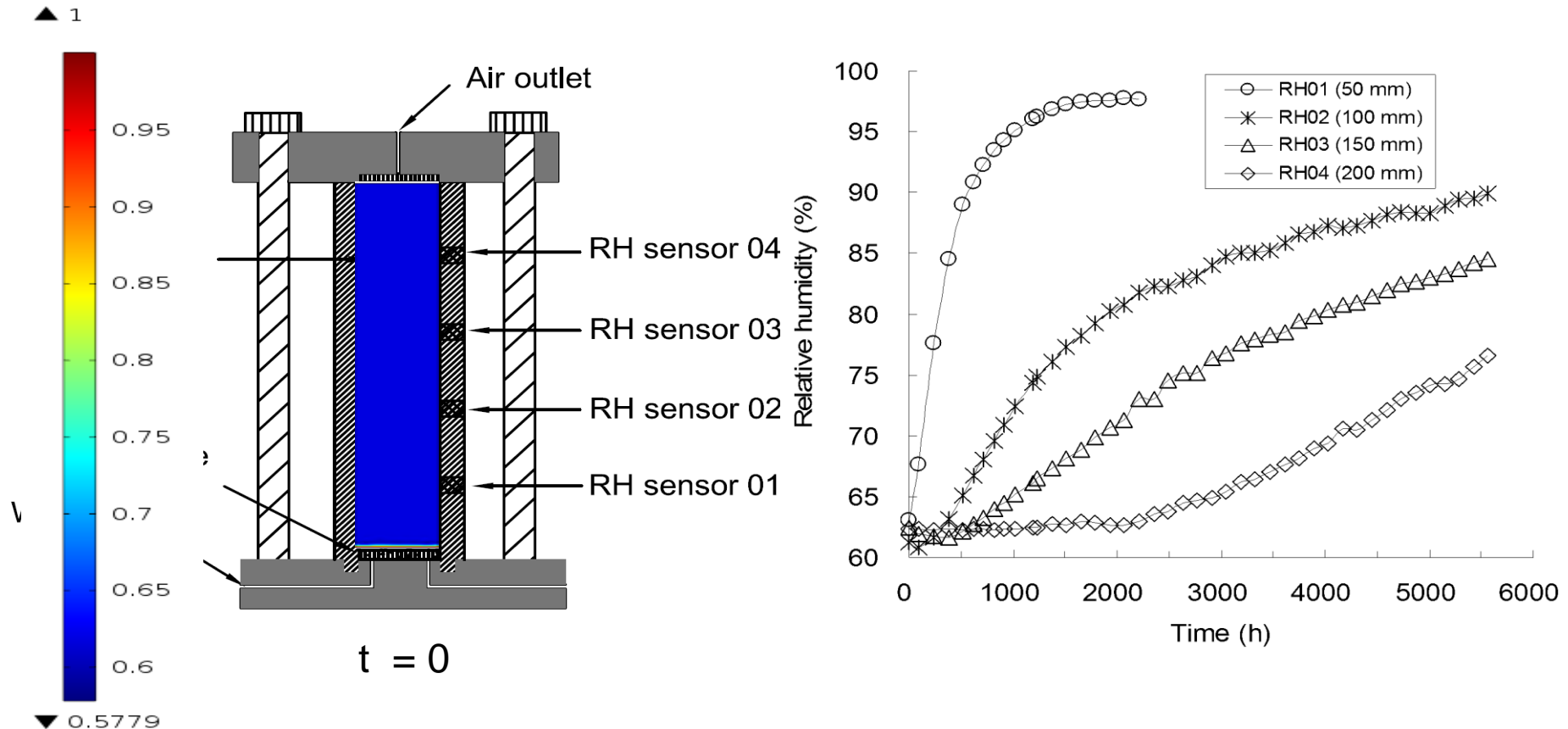
Infiltration test

- Focused on modelling of saturation process in bentonite MX-80 under **constant volume condition** (clay and quartz sand in dry weight proportions 70/30). It is mined out in Wyoming.



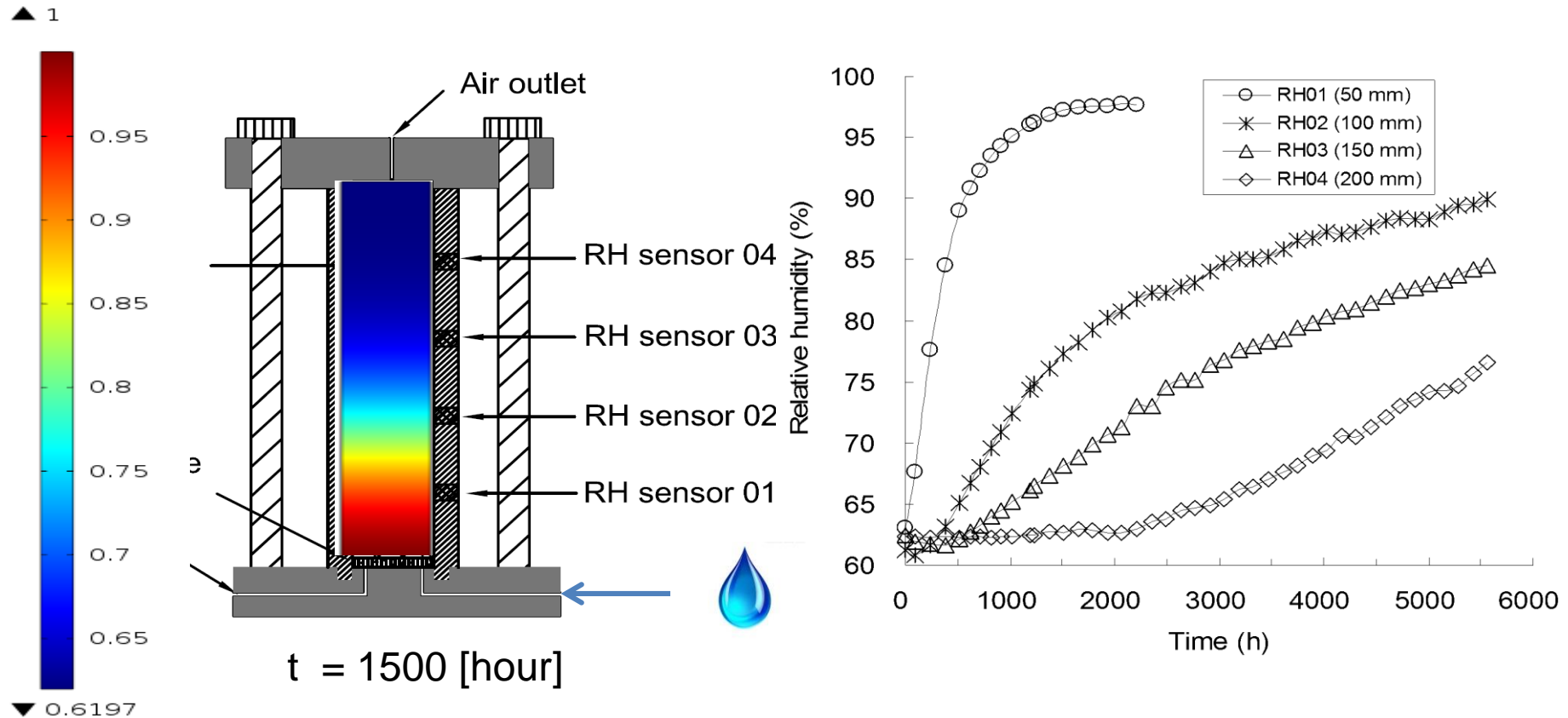
Experiments – Step 0

- Focused on modelling of saturation process in bentonite MX-80 under **constant volume condition**.



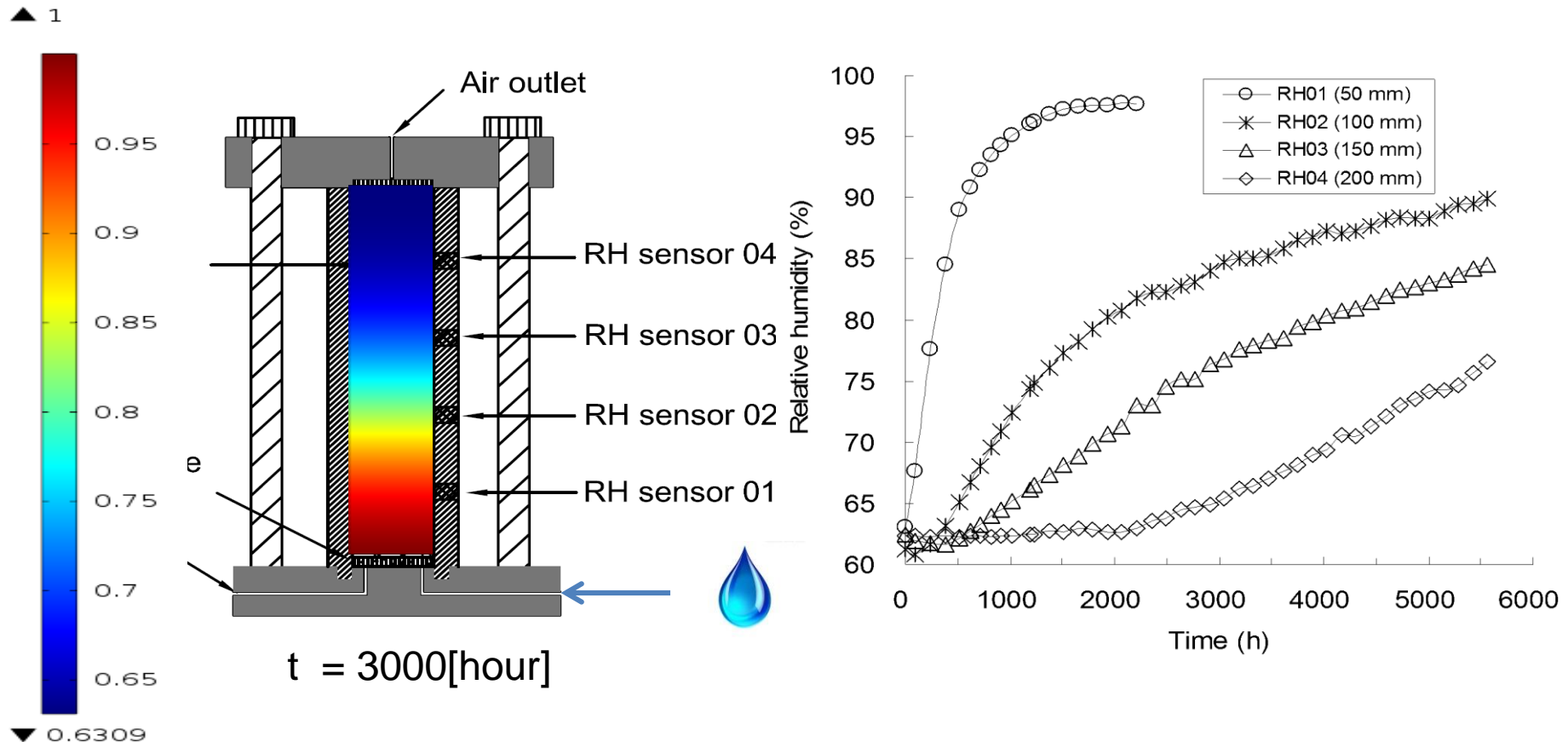
Experiments – Step 0

- Focused on modelling of saturation process in bentonite MX-80 under **constant volume condition**.



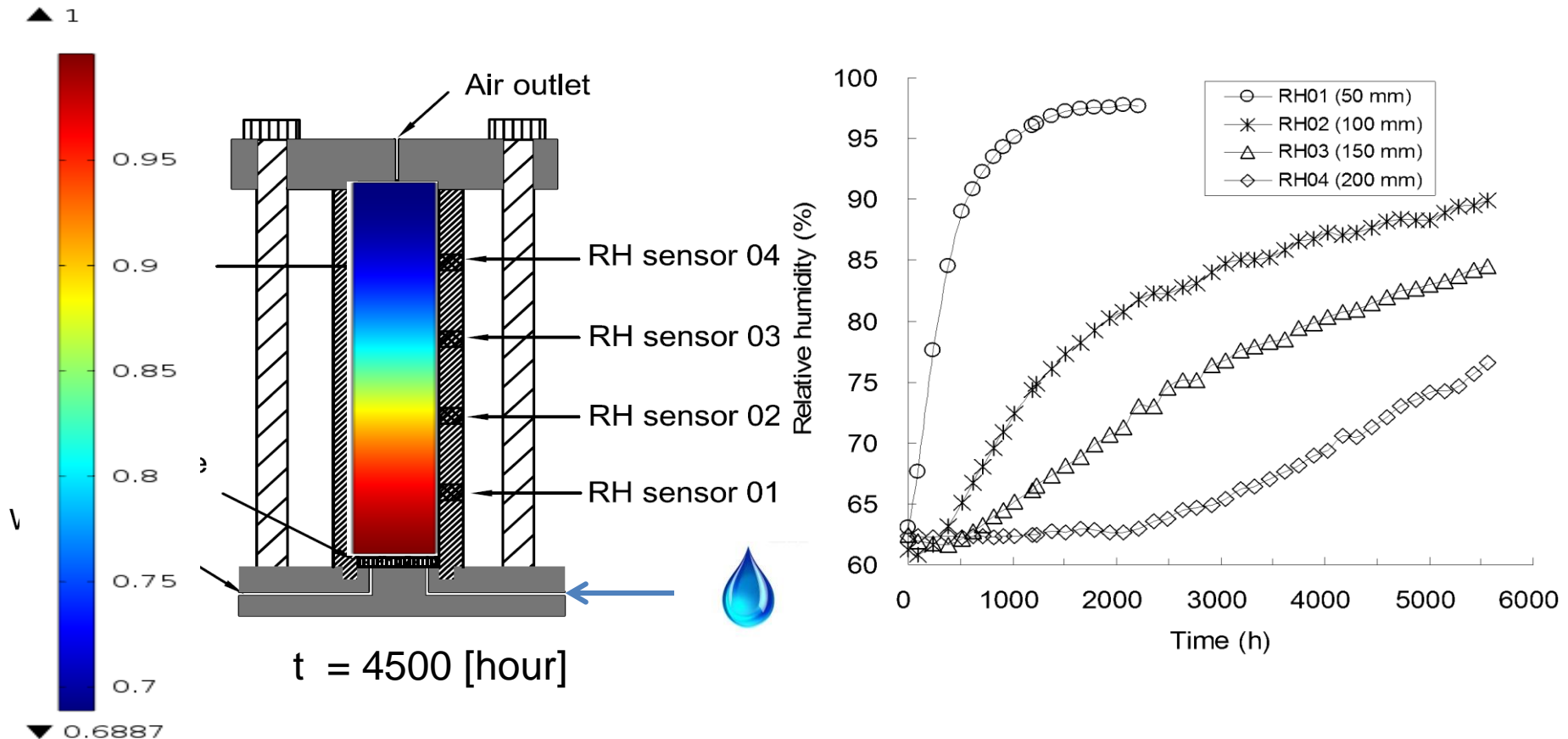
Experiments – Step 0

- Focused on modelling of saturation process in bentonite MX-80 under **constant volume condition**.



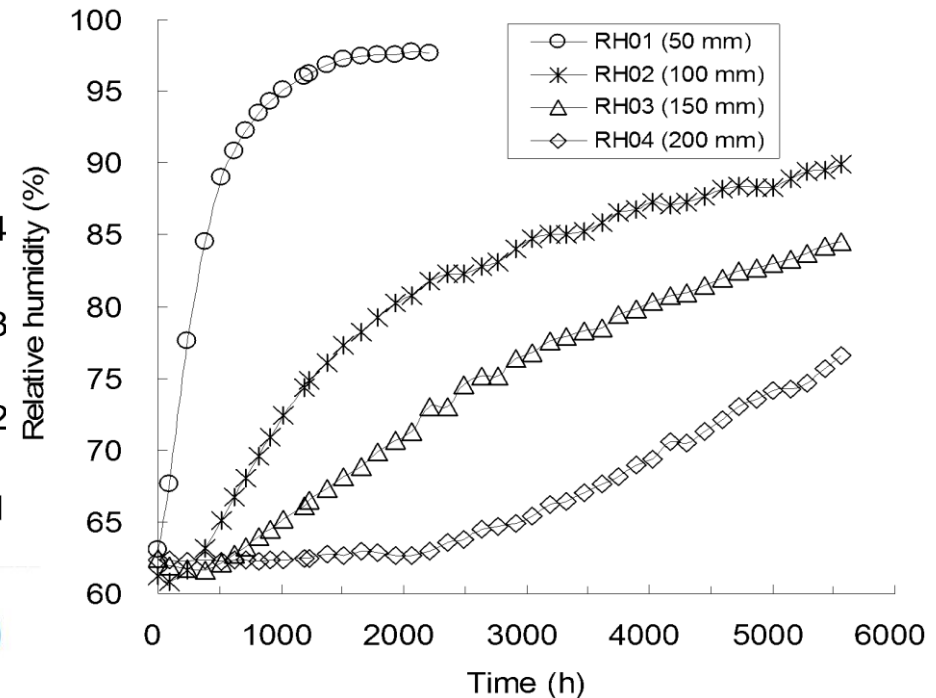
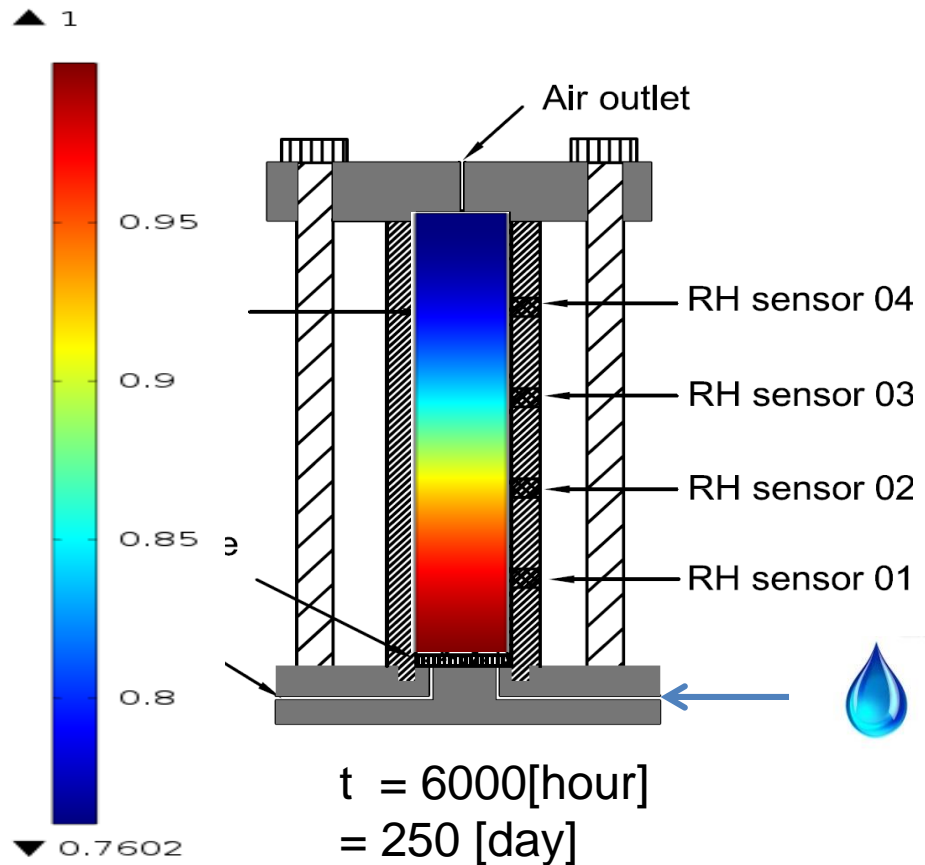
Experiments – Step 0

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Experiments – Step 0

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Mathematical model

Hydro

- H** unsaturated flow
 - Richard's equation
 - inputs: saturated and relative permeability, retention dependence

M Elasticity (linear/nonlinear)

Mechanics

HM coupling implemented COMSOL

- Biot-Bishop model,
 - effective stress, water squeezing due to porosity change
- permeability change (Kozeny),
- retention depending on deformation
- swelling deformation

HydroMechanics

Richards' equation

- represents the movement of water in **unsaturated soils**, and was formulated by Lorenzo A. Richards in 1931

$$\frac{\partial(\phi S_w \rho_w)}{\partial t} = \frac{\partial(\theta_w \rho_w)}{\partial t} = \nabla \cdot \left(\rho_w \frac{k_r k_{sat}}{\mu_w} \nabla (p_w + \rho_w g h_e) \right) + \rho_w q_w,$$

- Capillary pressure $p_c = \hat{p}_g - p_w$

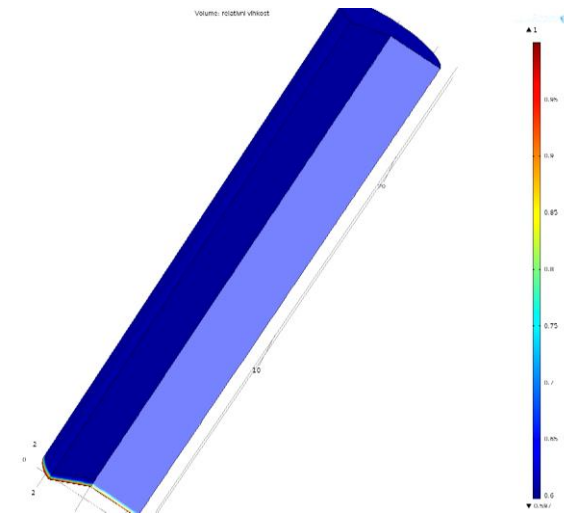
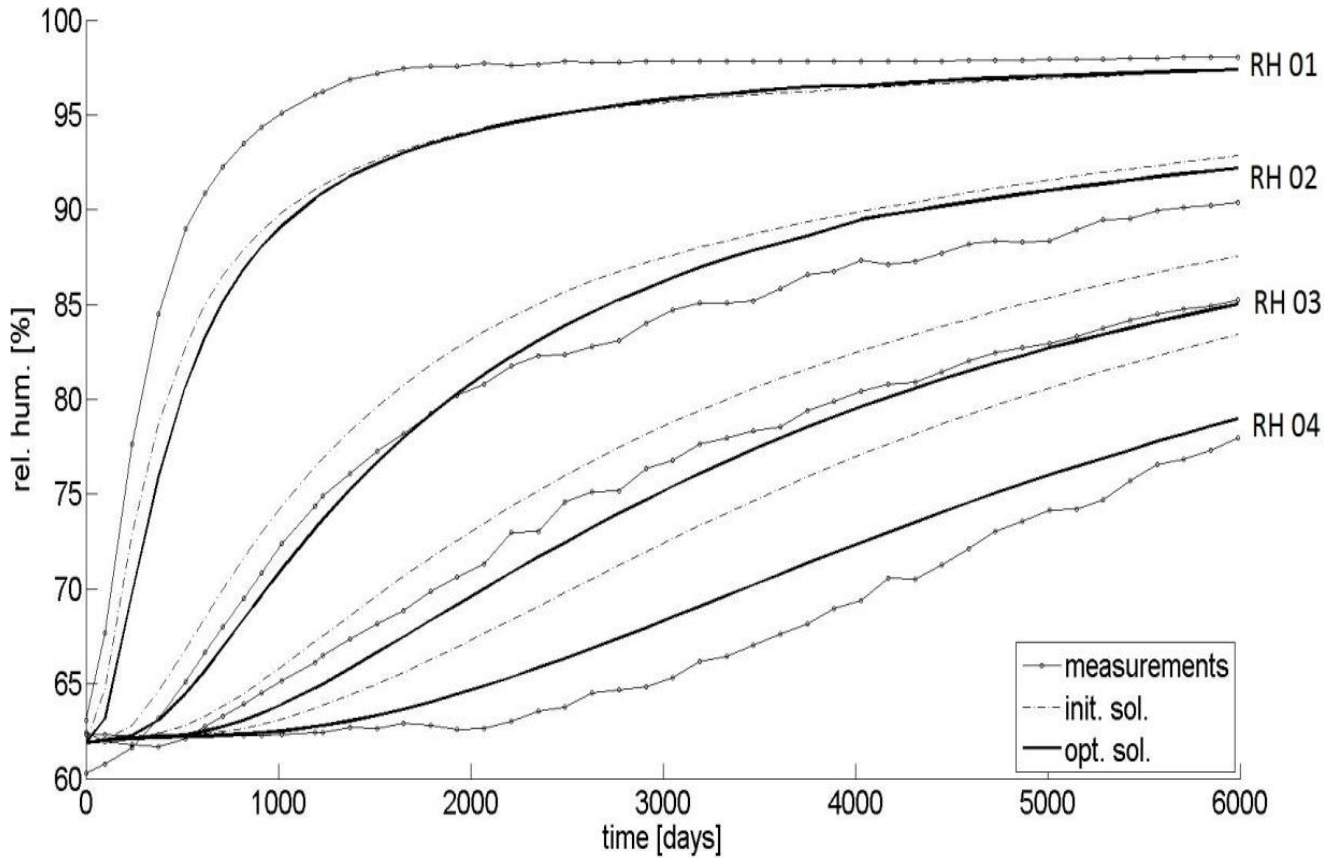
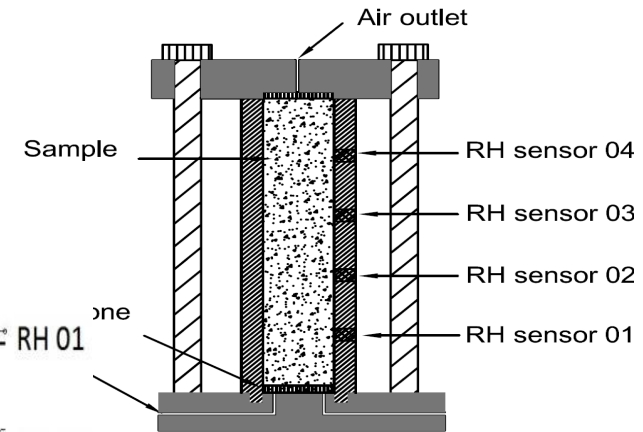
- Entries:

$$S_e = \begin{cases} (1 + |\alpha_{VG} \rho g p|^n)^{-m} = (1 + |\overline{\alpha_{VG}} p|^n)^{-(1-1/n)} & \text{if } p < 0, \\ 1 & \text{if } p \geq 0. \end{cases}$$

- Relative saturation $k_r(S) = S_e^k$

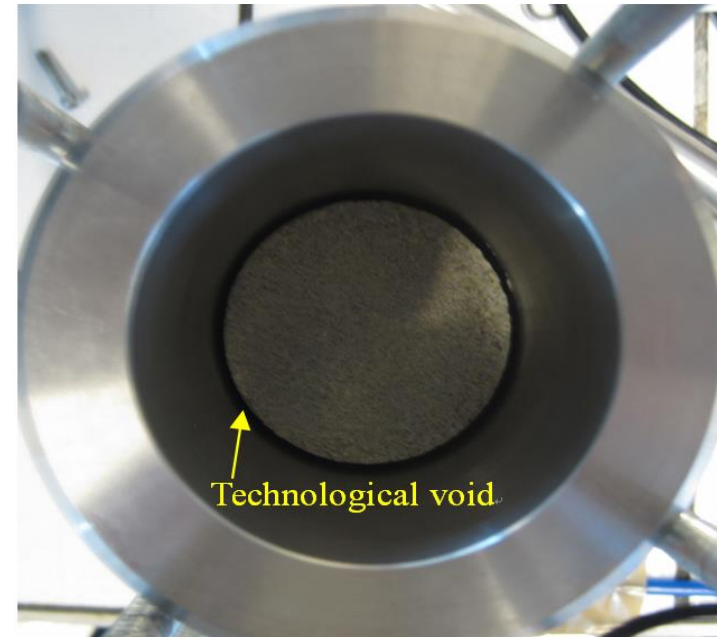
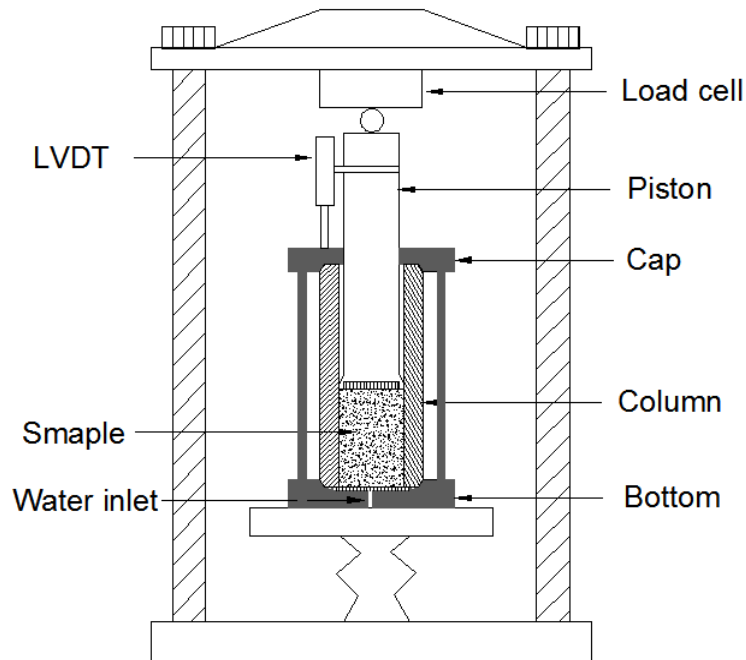
Results

Infiltration test



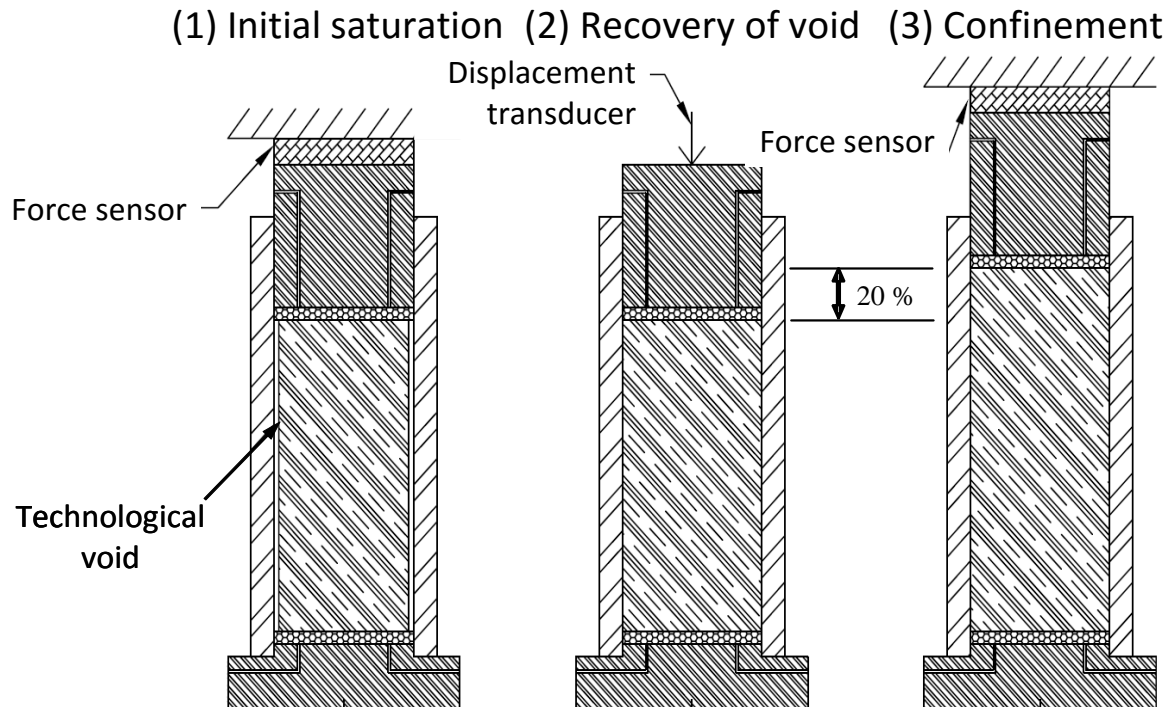
Experiments – Step 1

Similar to previous Step 0 - modelling of saturation process in bentonite MX-80, but under **unconstrained volume condition, HM !**

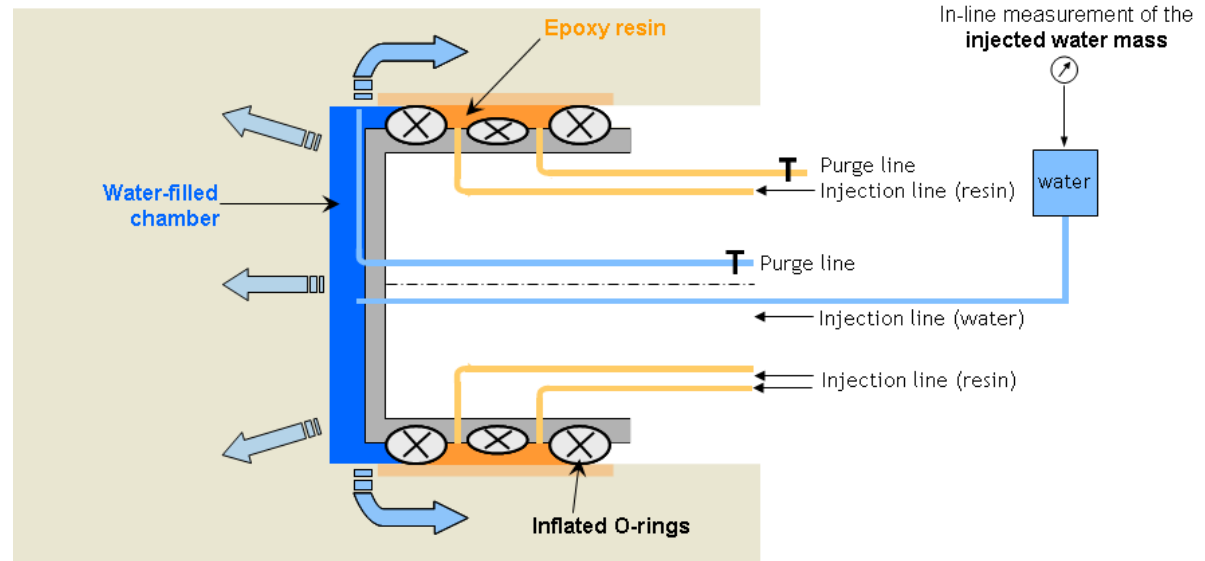


Experiments – Step 1

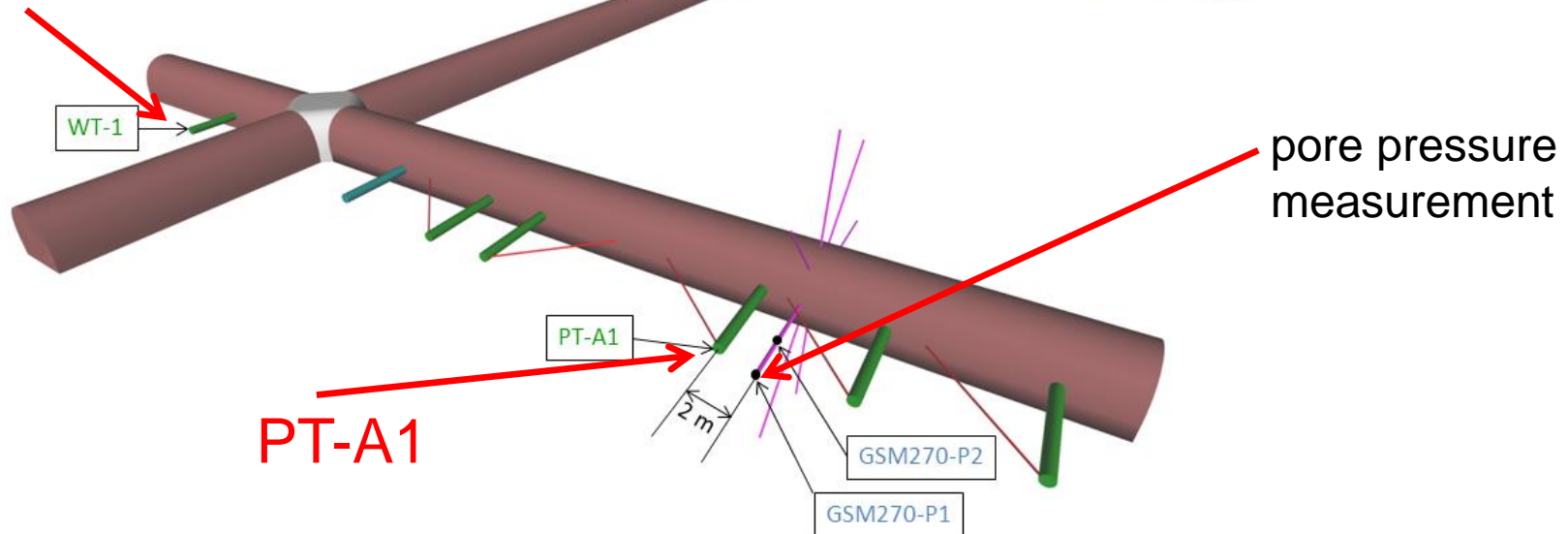
- Similar to previous Step 0 - modelling of saturation process in bentonite MX-80, but under **unconstant volume condition**.



In situ WT1 test PT-A1 test



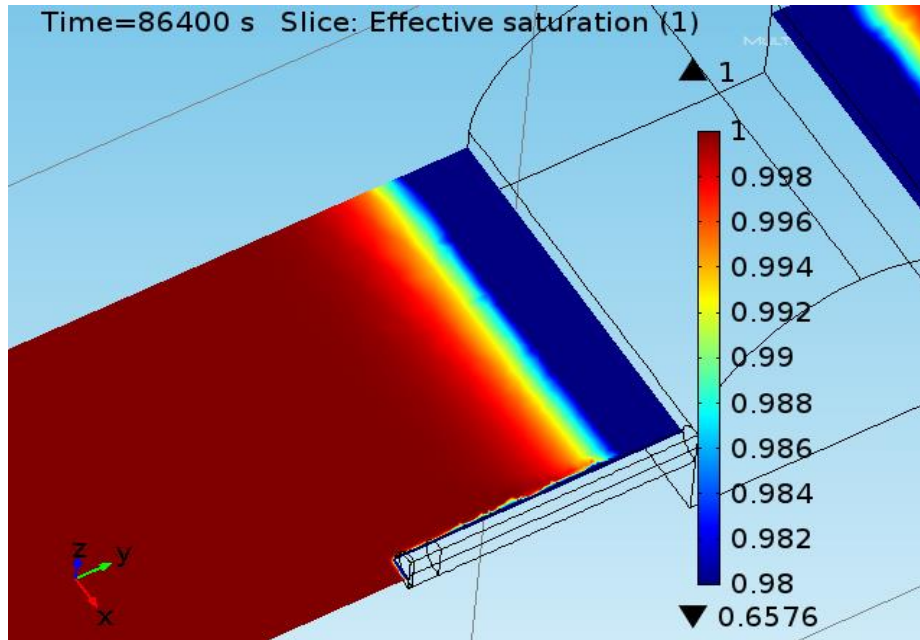
WT-1



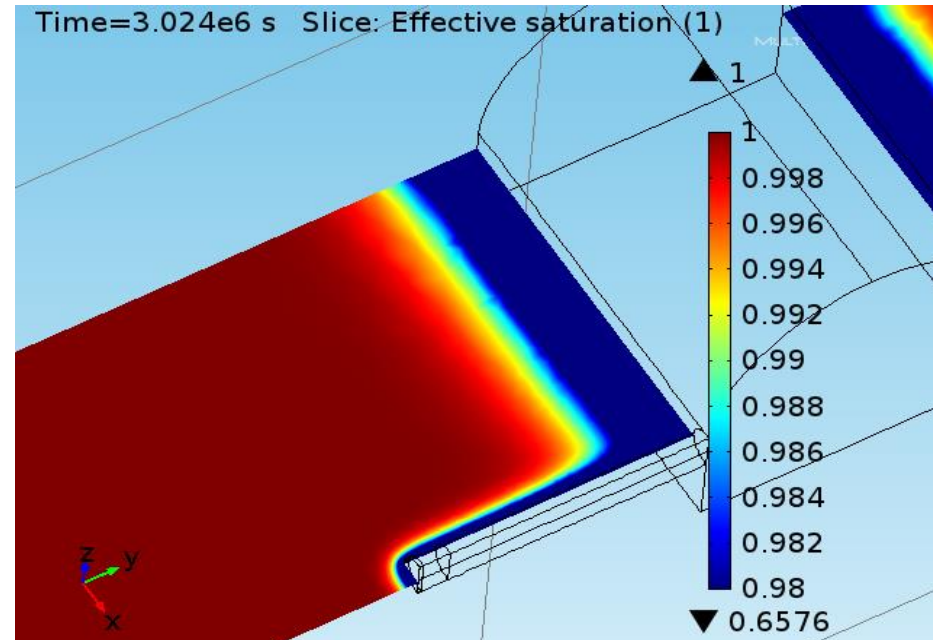
Results

3D model of the SEALEX WT-1 experiment

Effective saturation in rock 1 day and 35 days after borehole opening, pressure on the borehole wall $p=-25$ MPa.

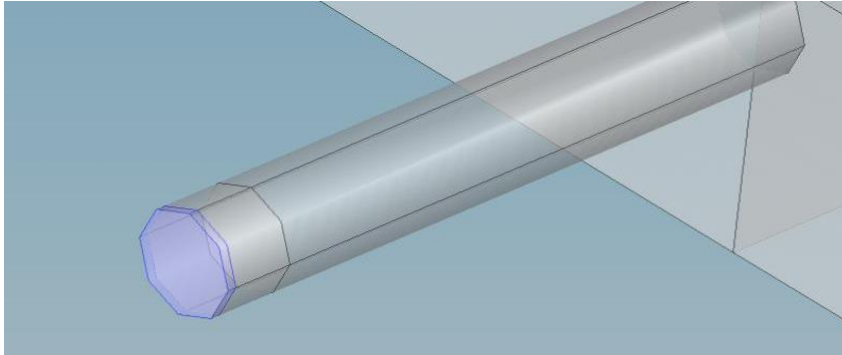


1 day after opening



35 days after opening [Pa]

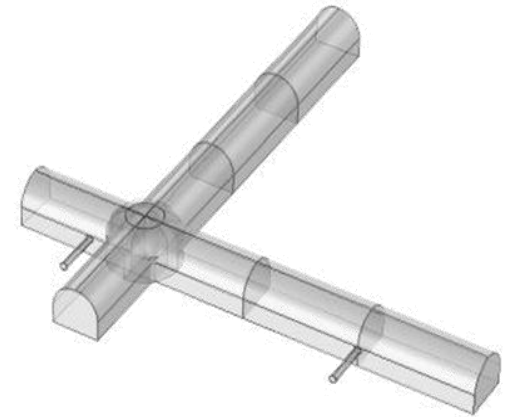
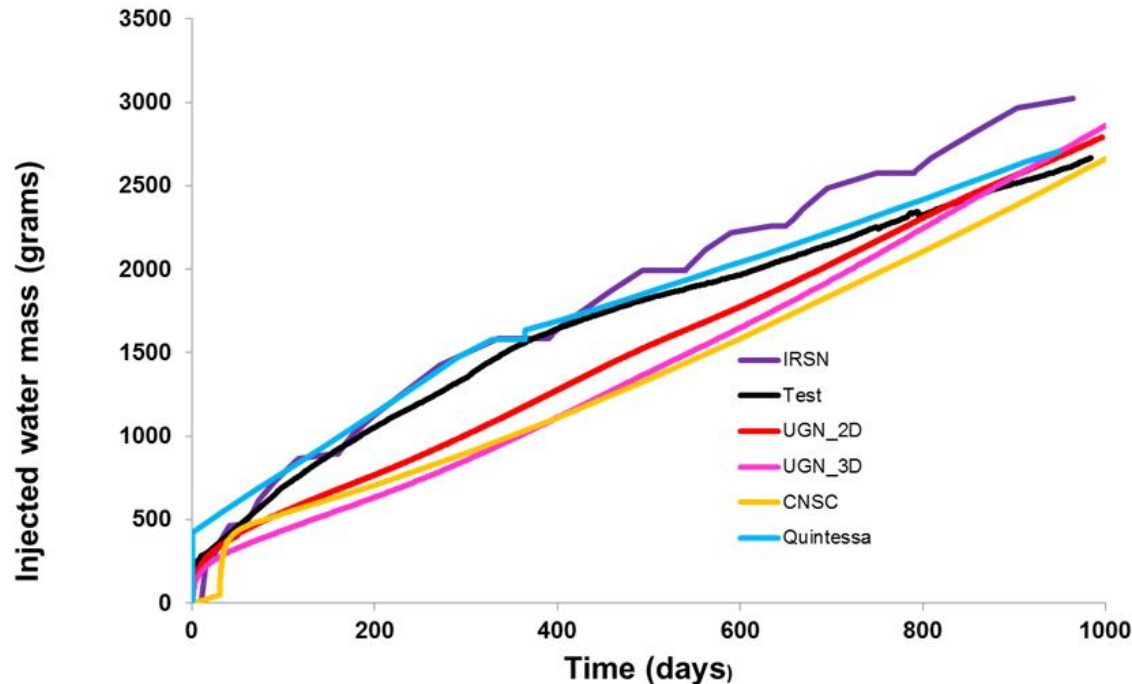
Experiments – Step 2 - results



$$Q = \iint_A \vec{v} \cdot d\vec{A}$$

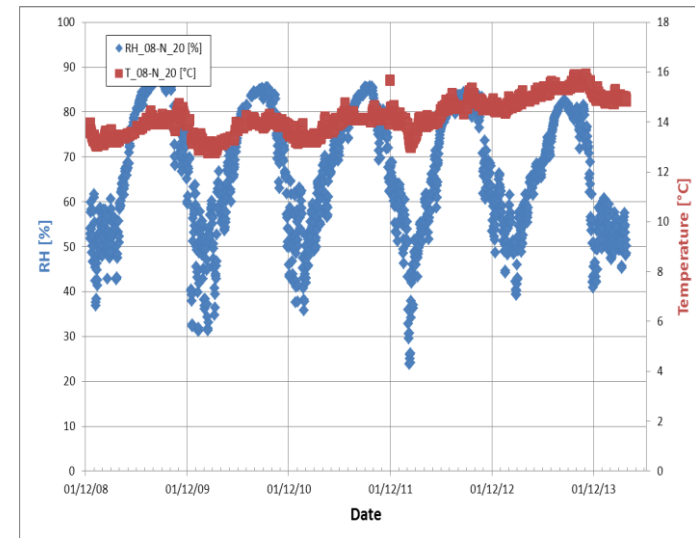
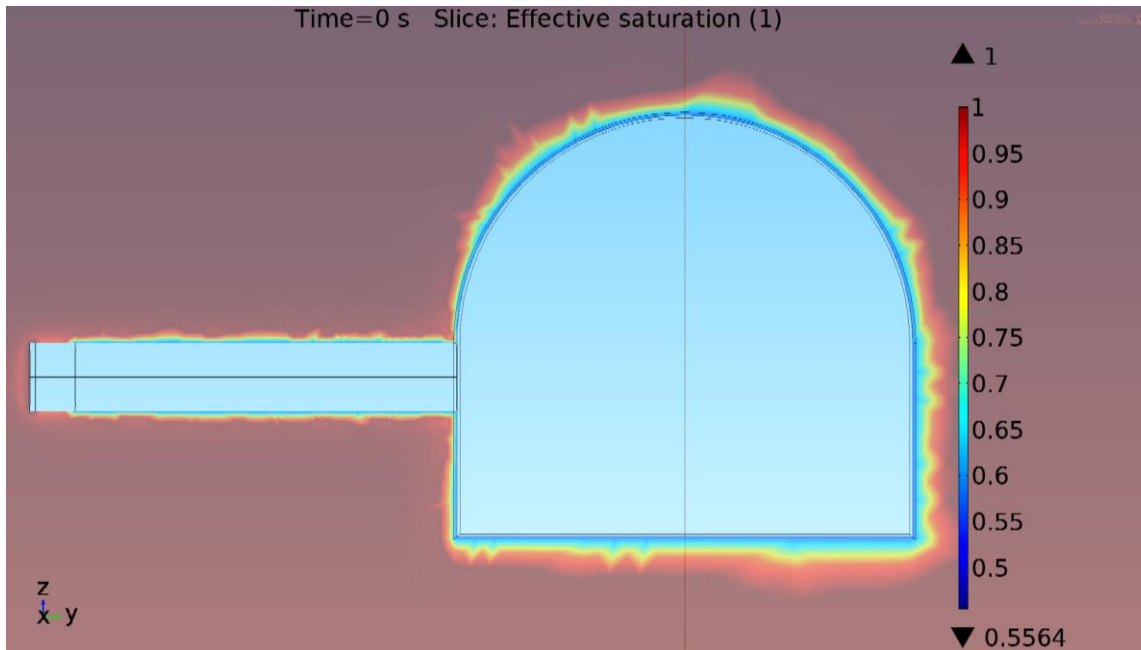
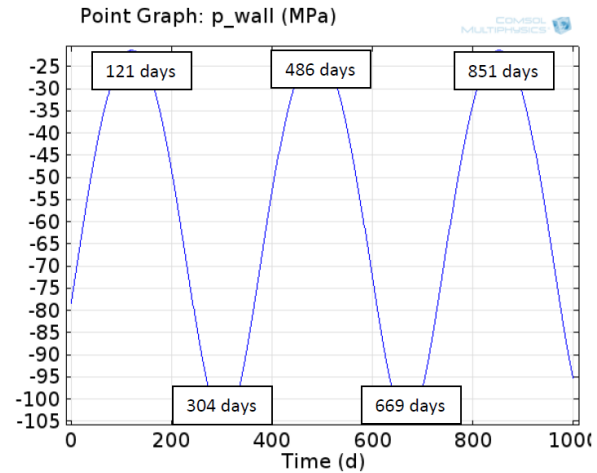
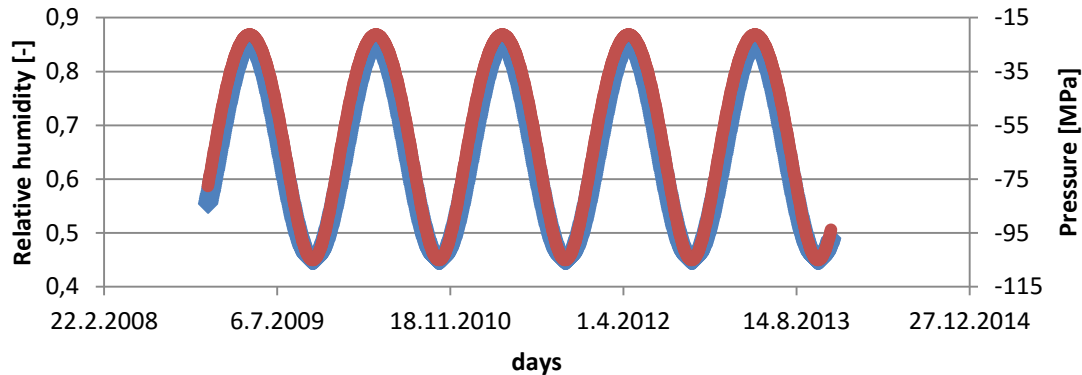
\vec{v} - flow velocity

\vec{A} - cross-sectional
vector area/surface



Results – boundary conditions

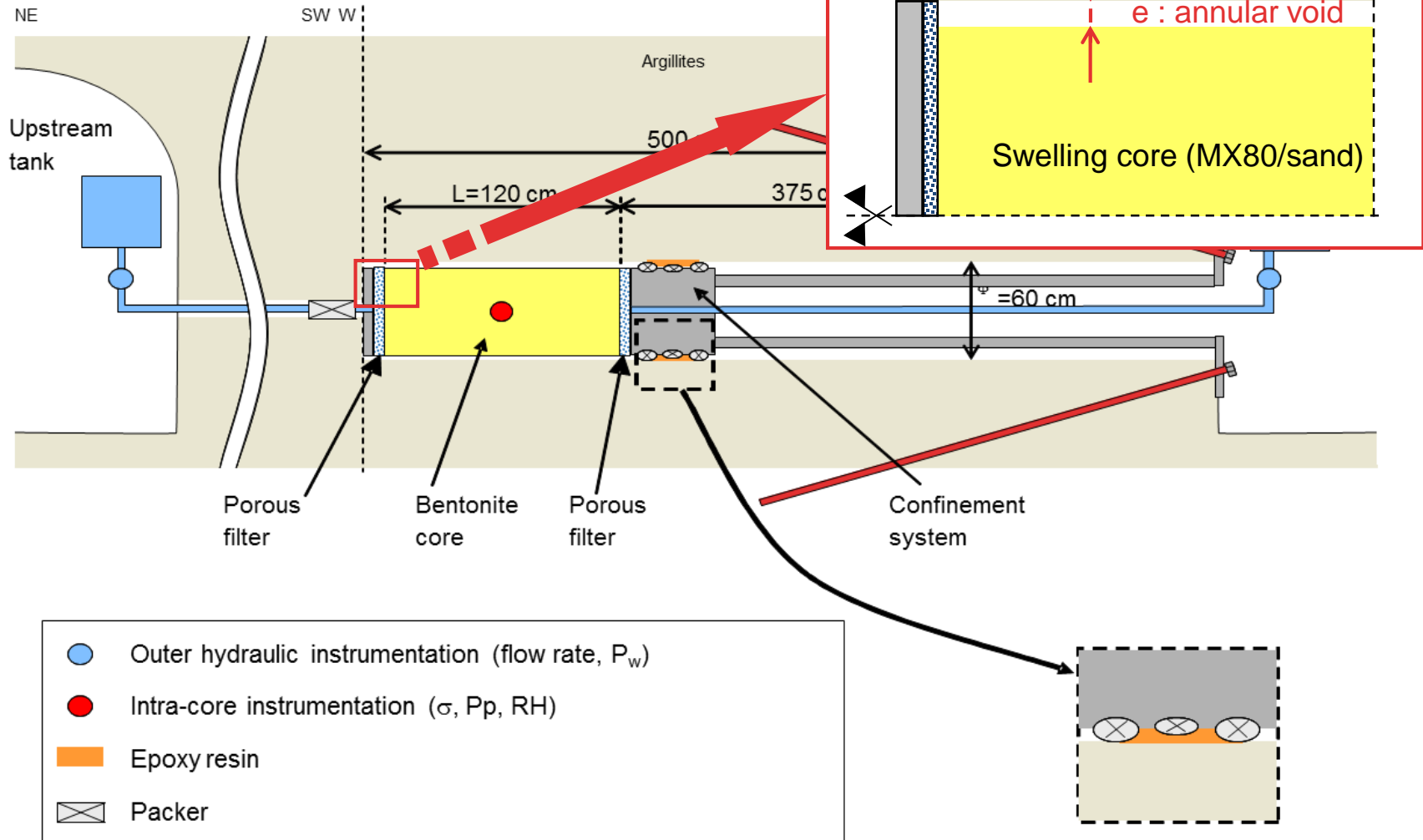
Relative humidity vs. capillary pressure



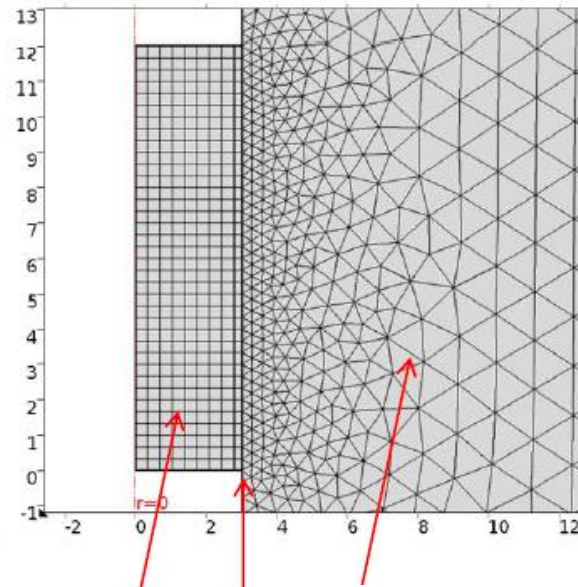
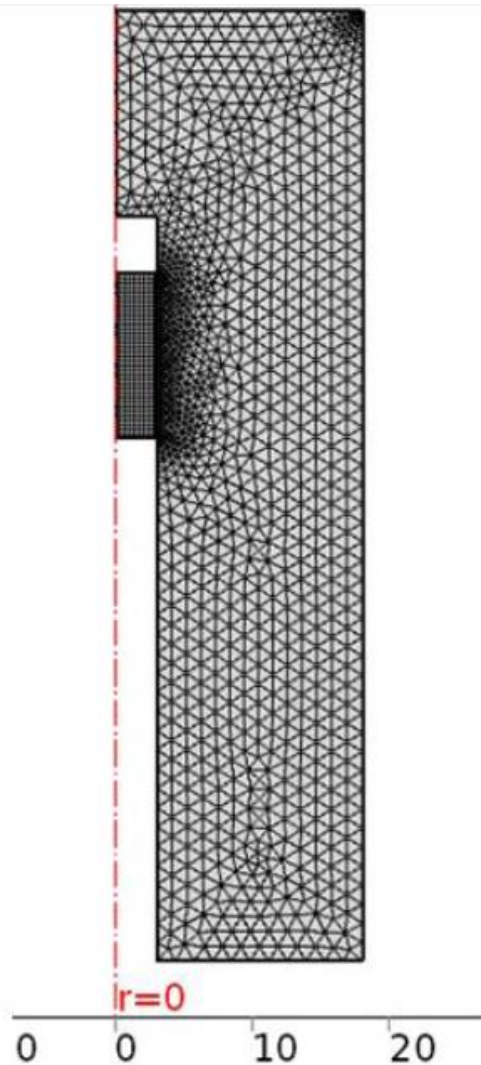
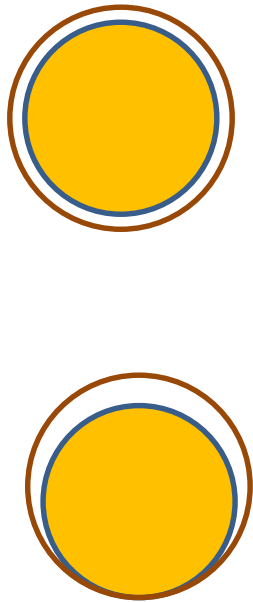
Effective saturation during year seasons

Step 3 – PT-A1 experiment

Intersection of PT-A1 experiment



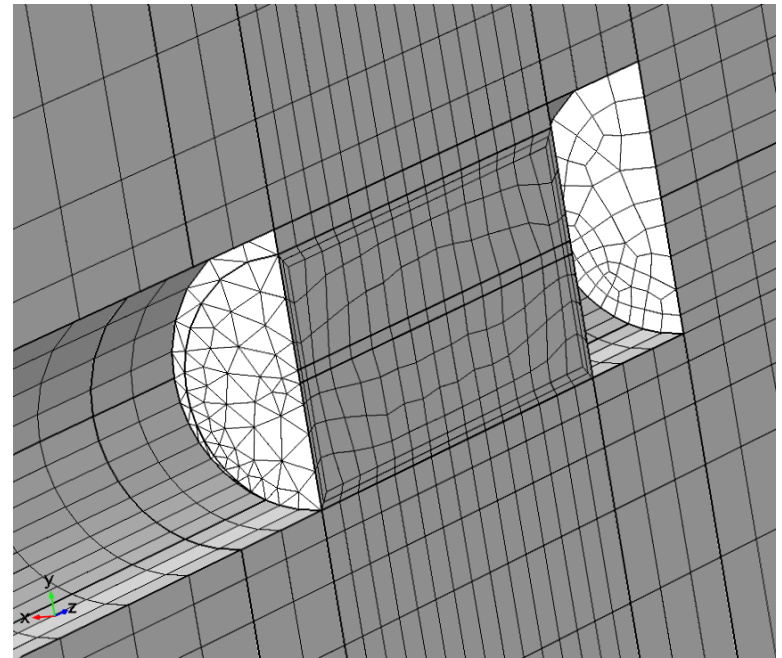
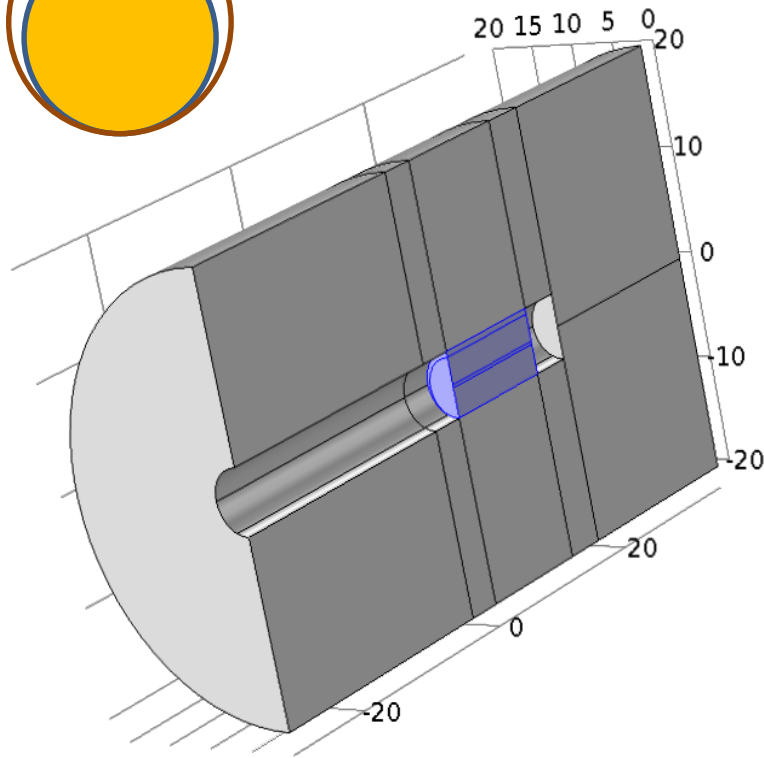
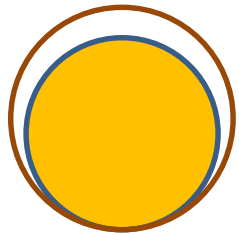
Axisymmetric model



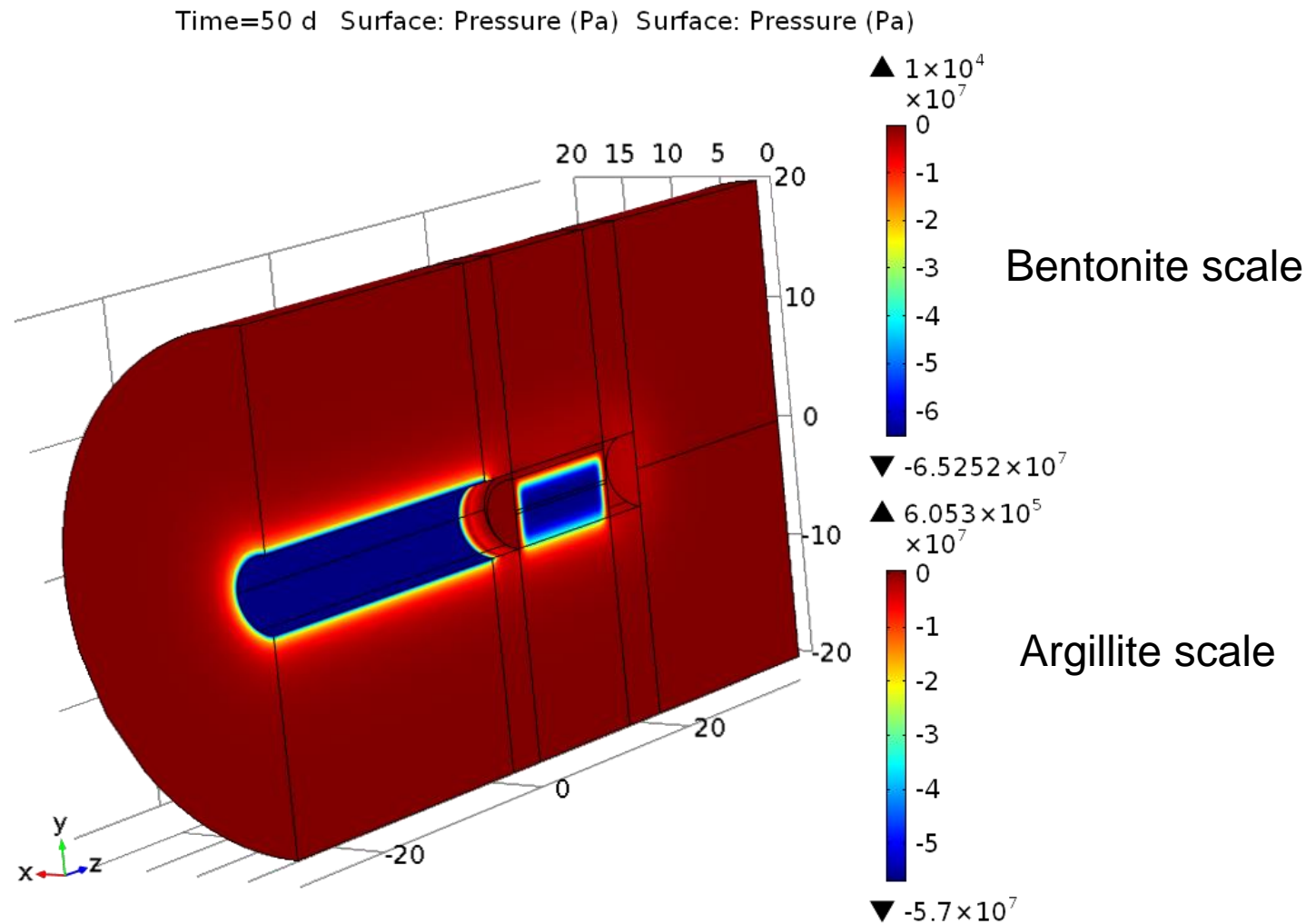
- B** = Bentonite mixture core
G = Gap, which is gradually behaving as a bentonite
A = Argillite

Model aiming at formulation of considered processes not at obtaining best coincidence with measurement,

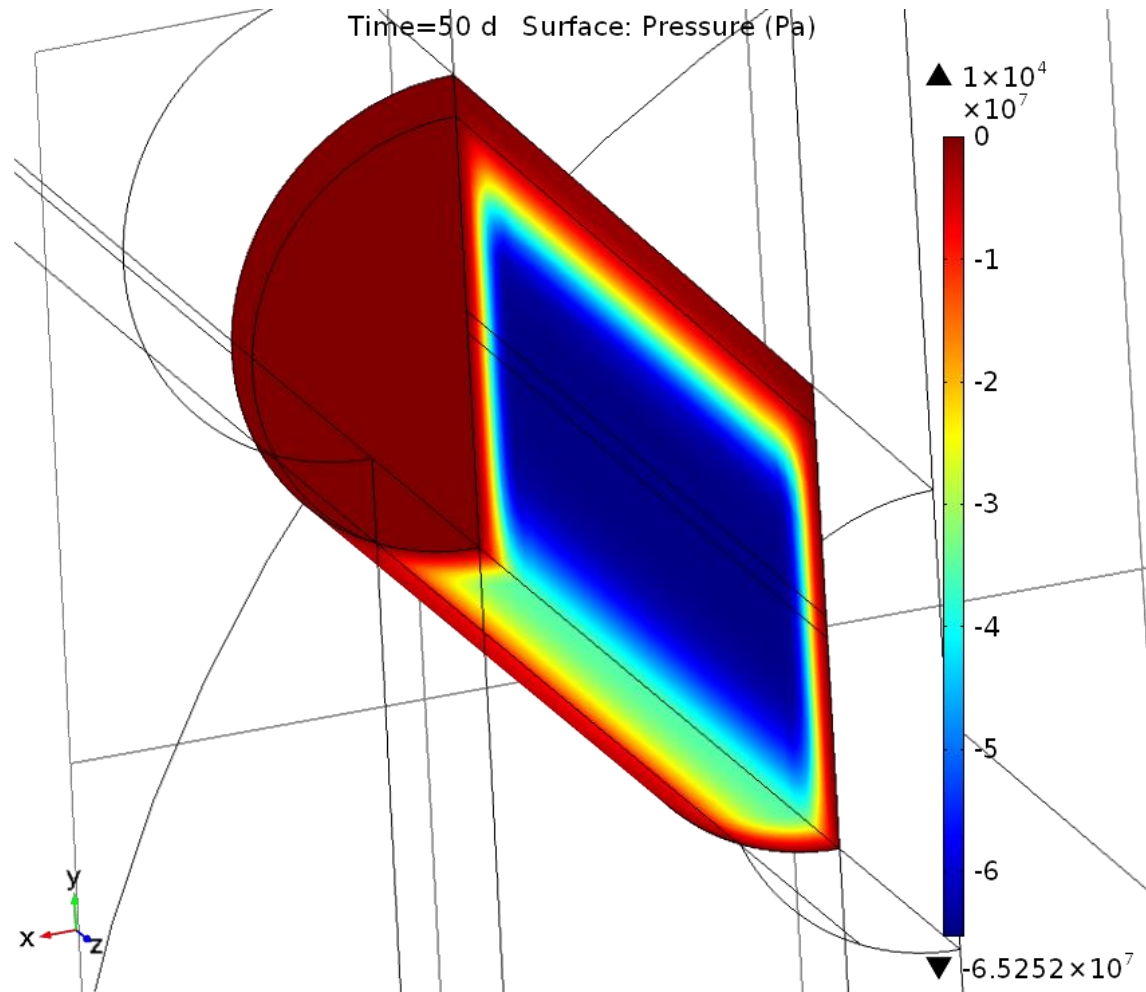
3D model with **nonsymmetric gap** and with **variable retention curve** depending on dry density



Pressure (suction) 50 days

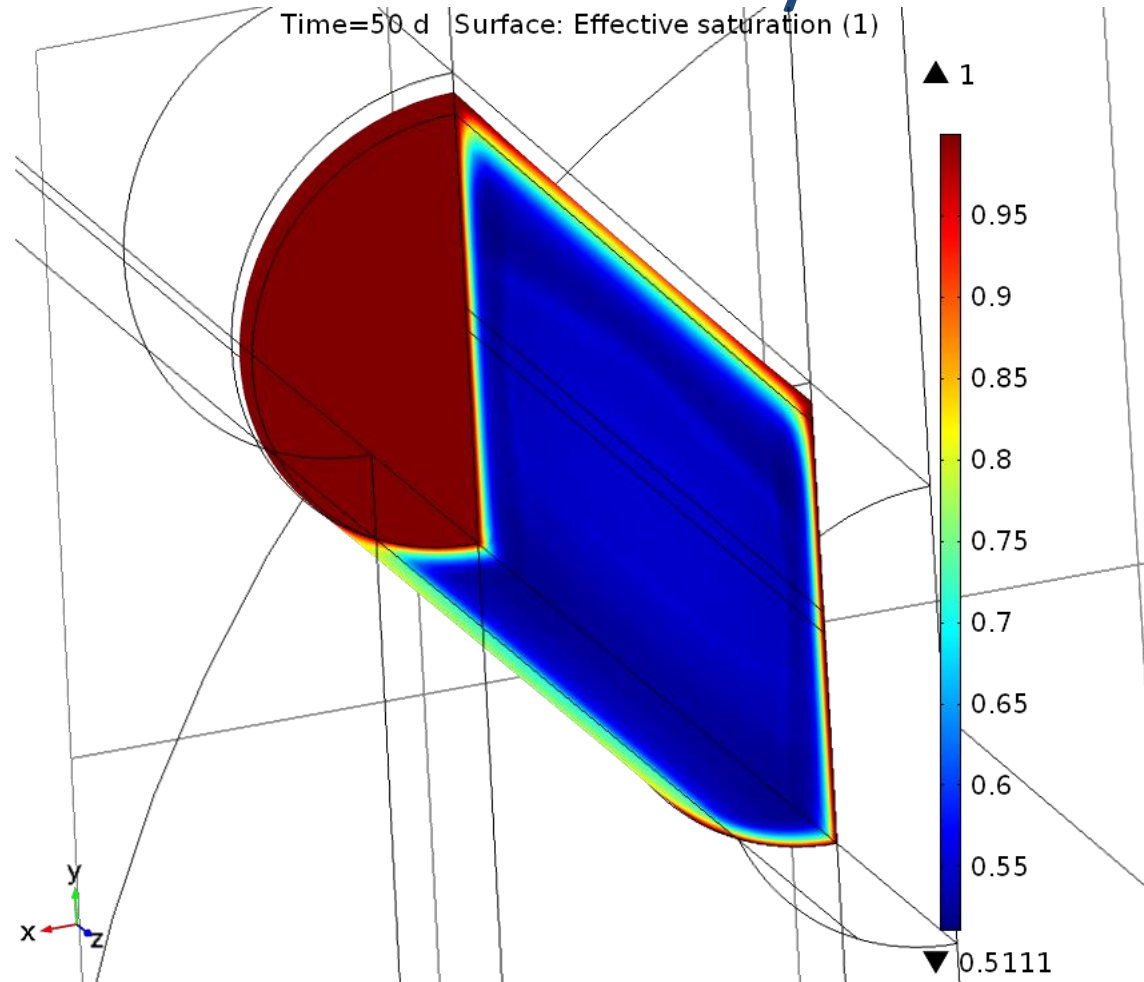


Pressure (suction) 50 days



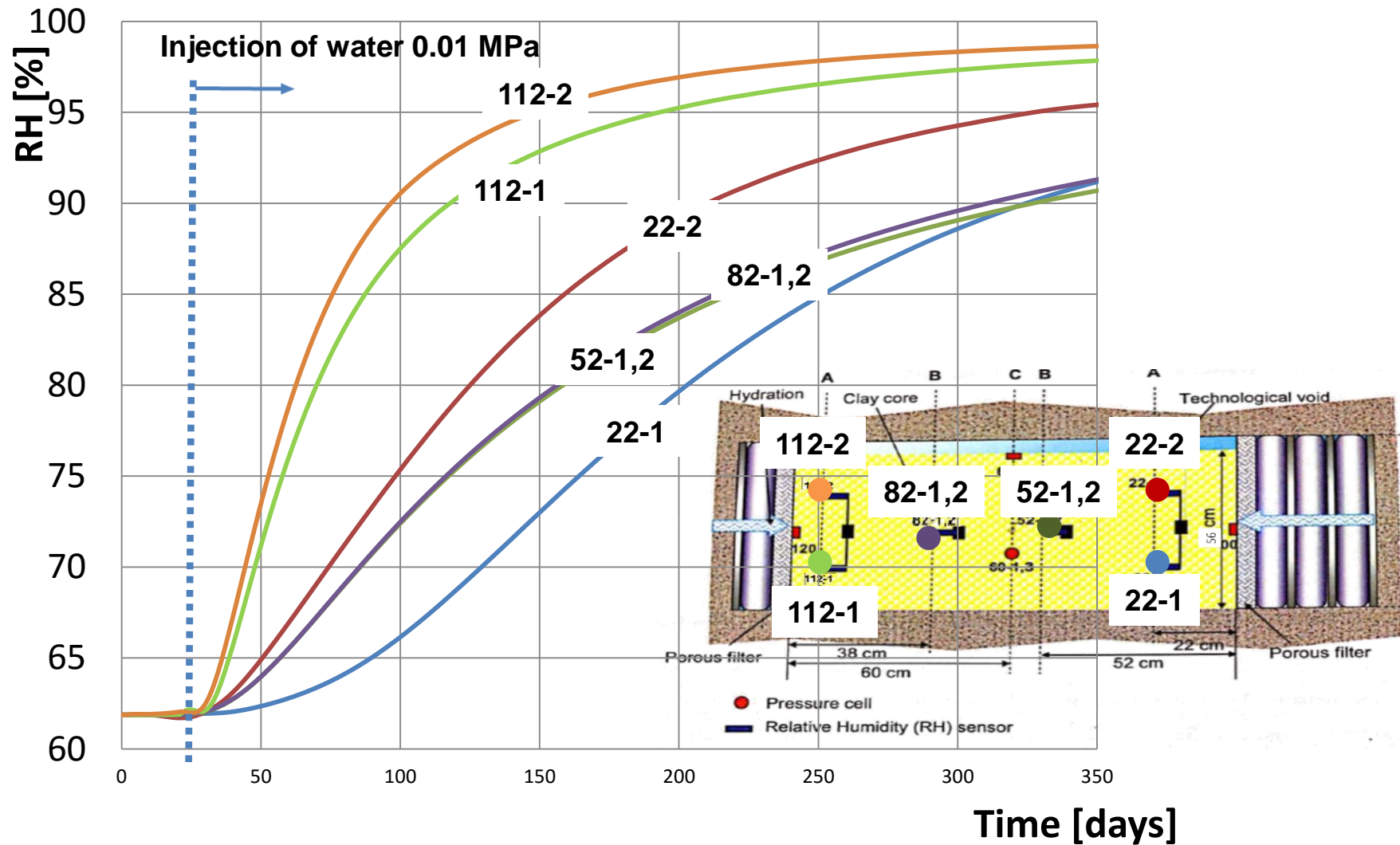
Suction decreasing, saturation depending also on pore size
can be increasing/decreasing

Effective saturation 50 days



Note: minimal value of saturation is $S_e=0.51$, which is below the initial state $S_e=0.57$ for $\rho_{dd}=1.94 \text{ Mg/m}^3$. Seems to be due faster swelling expansion than saturation.

Relative humidity - computations



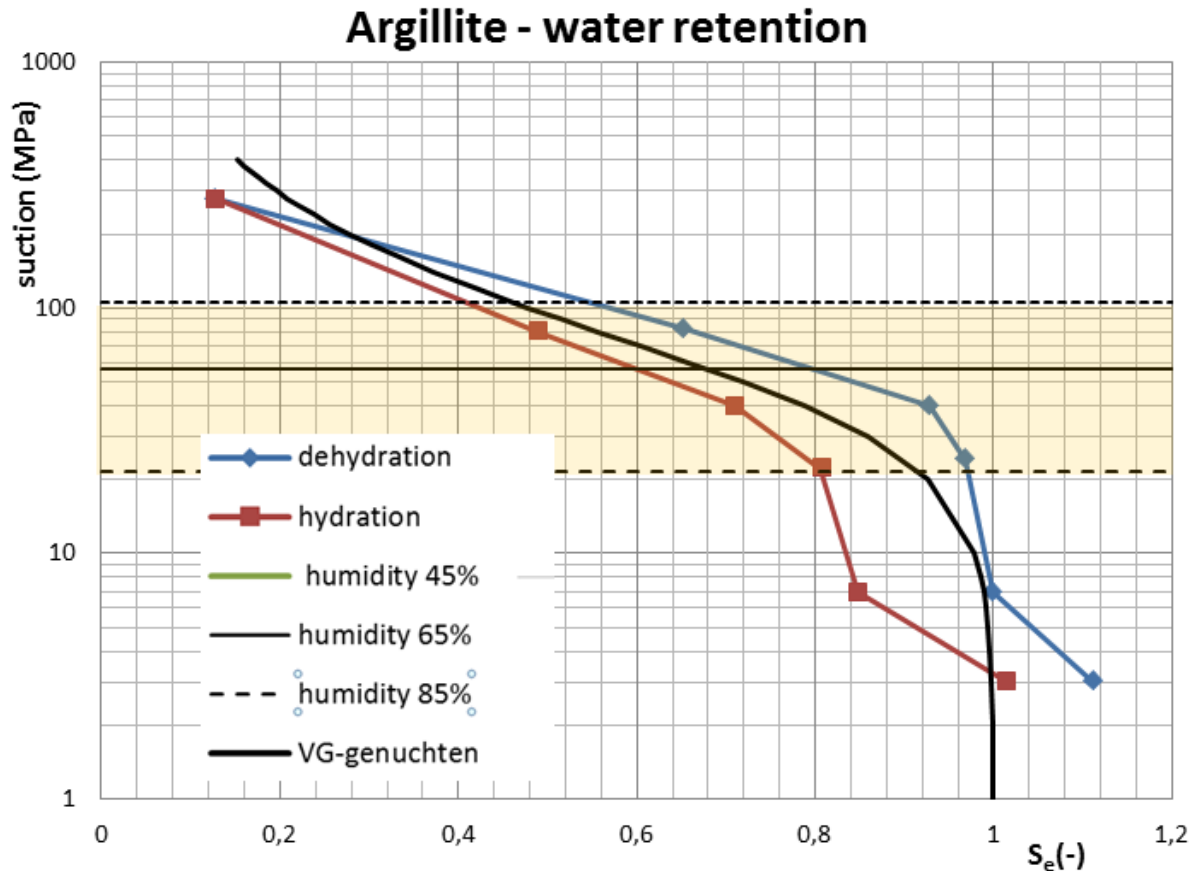
Thank you for your attention



Questions?

Considered processes

Water retention curve



provided data
for hydration/
dehydration
regimes

approximation
by common
Van Genuchten
curve

not hysteresis

*The marked layer corresponds to
humidity 45-85% in the gallery*

Argillite - elasticity with effective stress

$$\begin{aligned} -\nabla \cdot \sigma &= f_s \\ \sigma &= \sigma' - \alpha_B p I_\sigma \\ \sigma' &= C : \varepsilon(u) \end{aligned}$$

saturated flow

$$\begin{aligned} -\nabla \cdot \sigma &= f_s \\ \sigma &= \sigma' - \alpha_B \chi(S) p I_\sigma \\ \sigma' &= C : \varepsilon(u) \end{aligned}$$

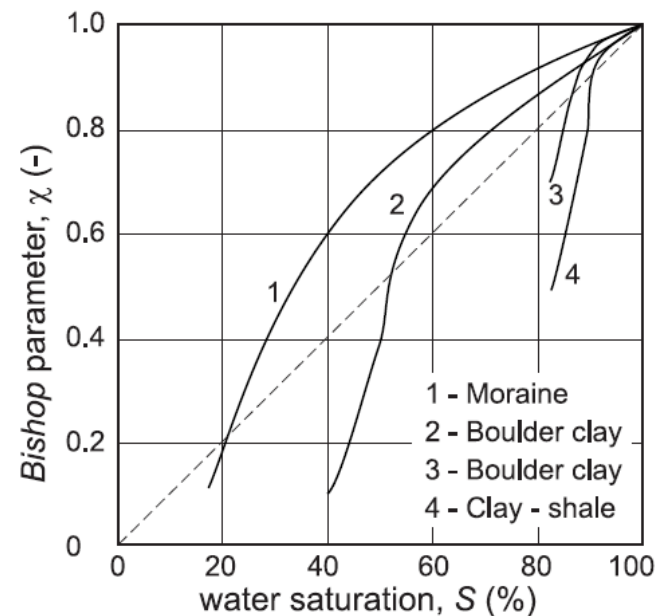
unsaturated flow

Biot-Willis constant $\alpha_B = 0.75$

Bishop function $\chi(S) = S$

C anisotropic linear elasticity

STEP 3 – now only Hydro

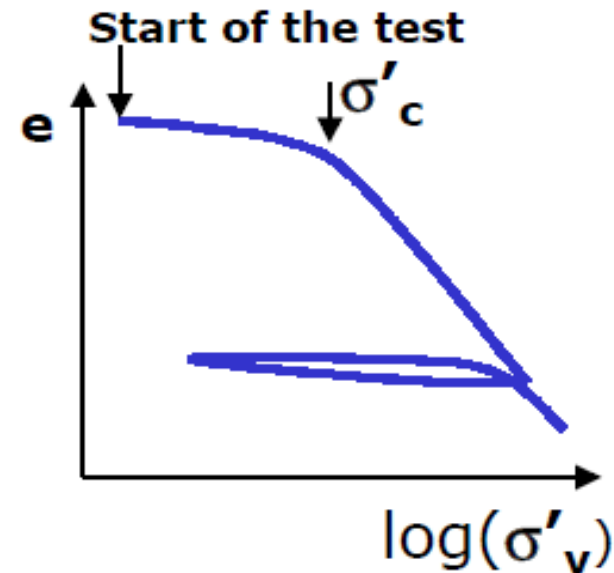


Bentonite – nonlinear elasticity

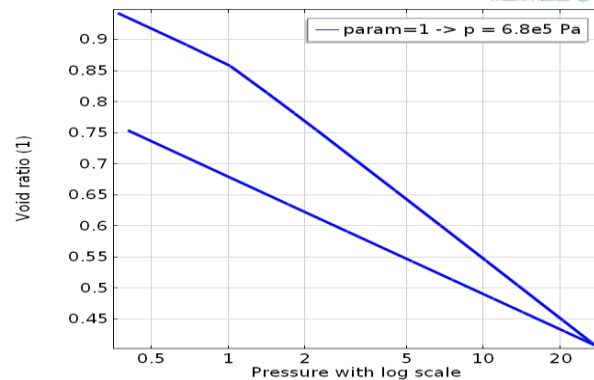
$$\sigma_v = - \frac{E(1-\nu)}{(1+\nu)(1-2\nu)} \varepsilon_v$$

$$e = e_0 + \varepsilon_v(1 + e_0),$$

$$E = E(e) = A \cdot 10^{B \cdot e}$$

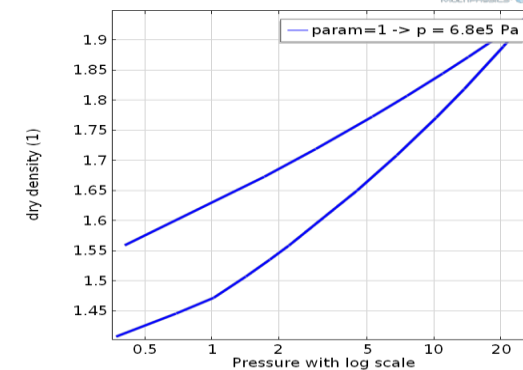


vs. log of the pressure during an isotropic compression test.



$$e = \frac{\rho_s}{\rho_d} - 1 \Rightarrow$$

vs. log of the pressure during an isotropic compression test.



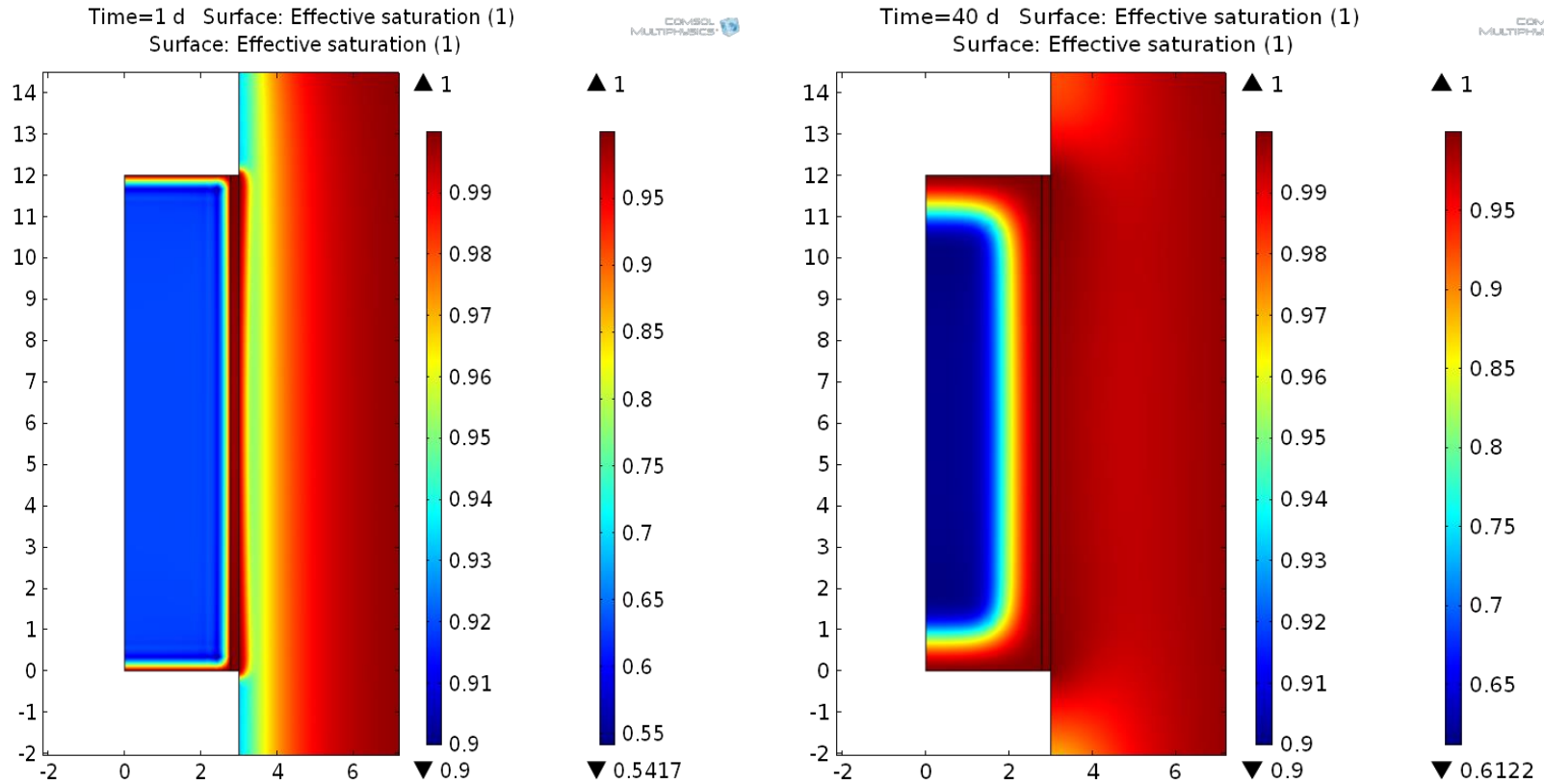
Bentonite – effective stress and pore space change

$$\sigma = \sigma' - \alpha_{BW} \chi(p) \cdot I, \quad \sigma' = C : \varepsilon$$

$$\chi(p) = \max\{p_w, p_a\} \sim \begin{cases} p_w & p_w > 0, \\ 0 & \text{otherwise.} \end{cases}$$

$$\frac{\partial \phi}{\partial t} = \frac{\partial}{\partial t} \left(\frac{\phi_0 + \text{tr}(\varepsilon)}{1 + \text{tr}(\varepsilon)} \right) = \frac{\partial(\text{tr}(\varepsilon))}{\partial t} \frac{(1 - \phi_0)}{(1 + \text{tr}(\varepsilon))^2}.$$

Evolution of the saturation – 1 and 40 days



Thank you for your attention !